

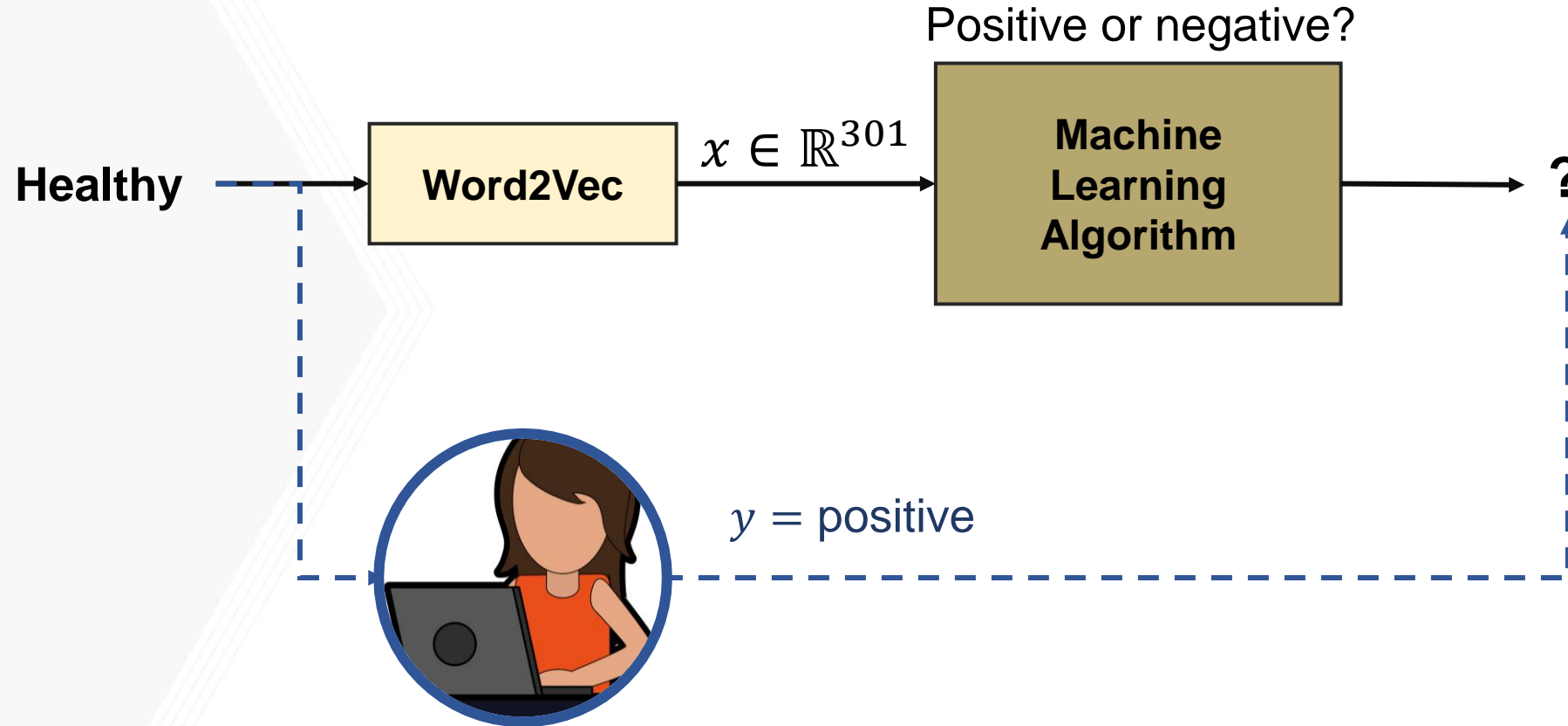
# Enhancing Human-in-the-Loop Learning for Binary Sentiment Word Classification

Belén Martín-Urcelay, Christopher R. Rozell, Matthieu R. Bloch

December 17, 2024

# 1. Background Motivation

How can ML algorithms learn to classify words **without exhausting human patience?**

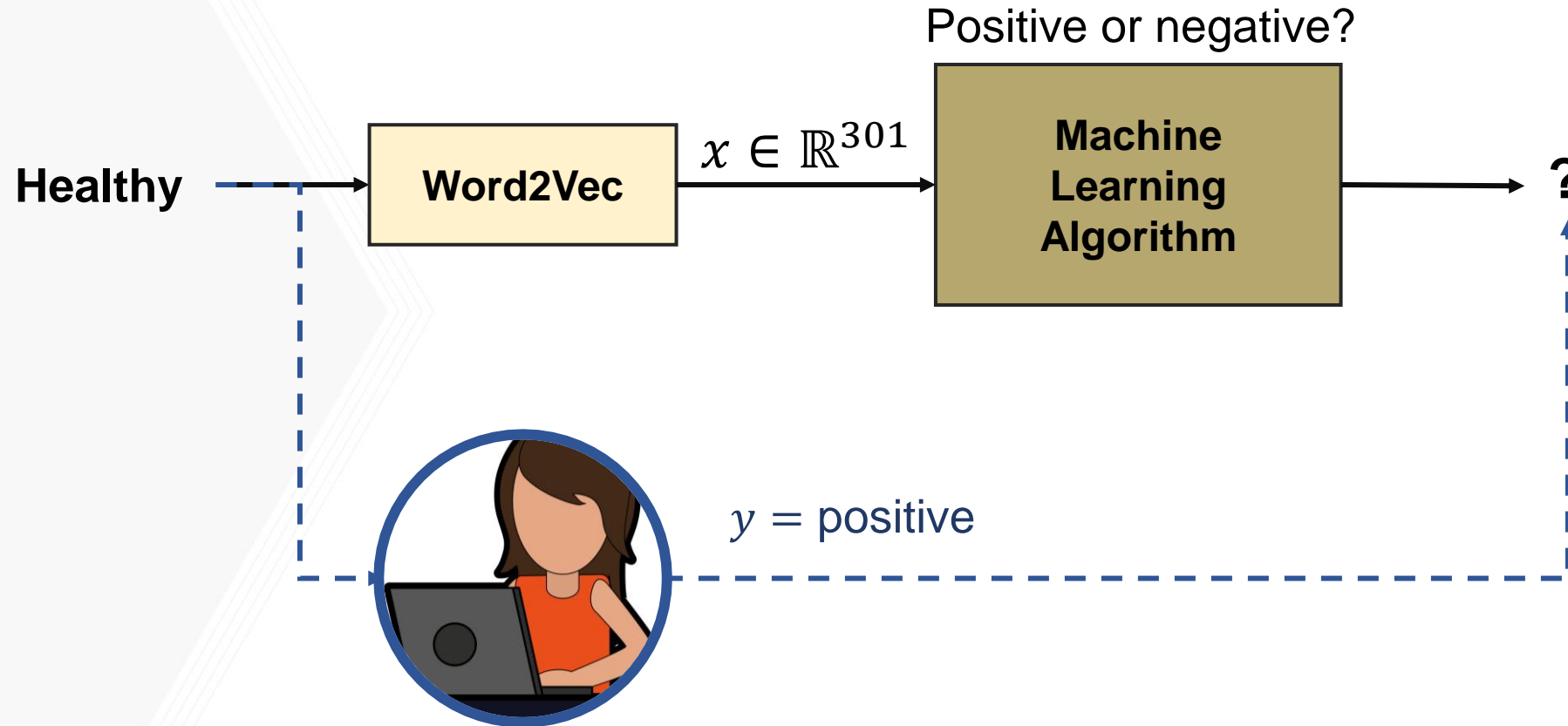


Supervised learning: training with labels from humans

Slide 2 of 19

# 1. Background Motivation

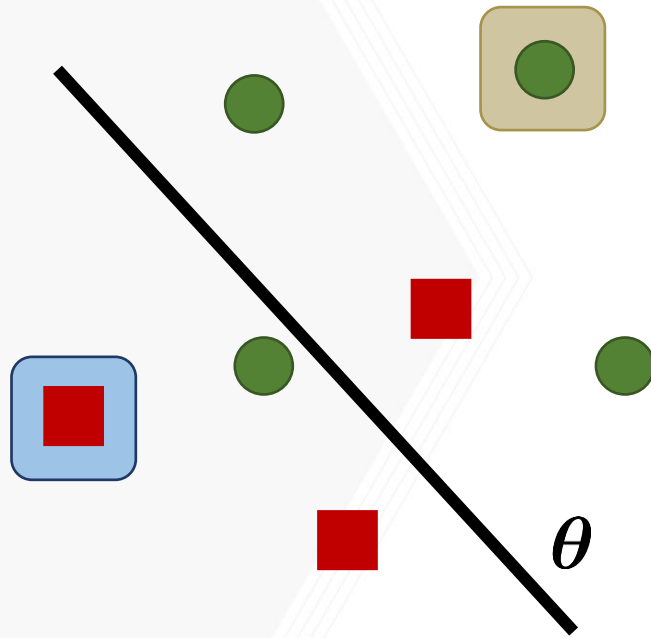
How can ML algorithms learn to classify words **without exhausting human patience?**



❑ Could we get **more information** from the human?

## 2. More Information

Queries must be human and mathematically interpretable



- : Positive word embedding
- : Negative word embedding
- $\theta$  : Word Classifier

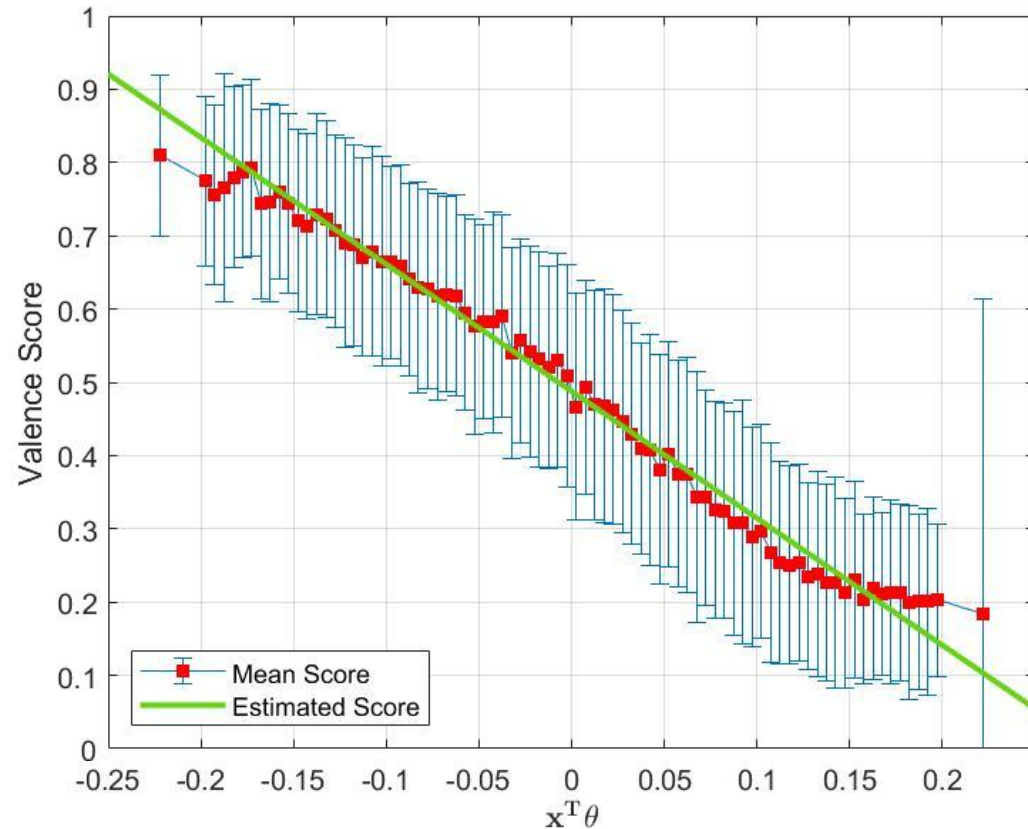
“Select the example that you find...”

- Query: “... most **positive**”
- Query: “... most **negative**”

**Hypothesis:** Human answers depend on the distance to the ground truth

## 2. More Information Valence vs Distance to $\theta$

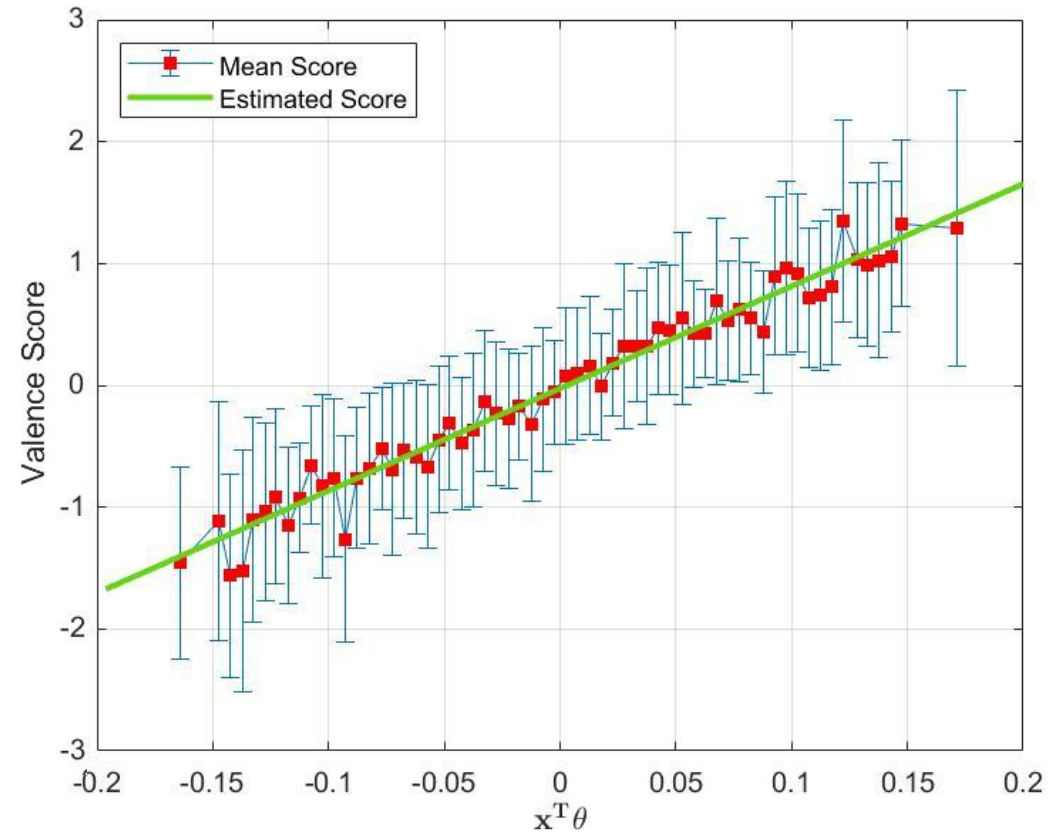
**NRC-VAD Lexicon**



$$\mathbb{E}[\text{score}(\mathbf{x})|\boldsymbol{\theta}] = -1.73(\mathbf{x}^T \boldsymbol{\theta}) + 0.49$$

$\mathbf{x}$ : Word embedding     $\boldsymbol{\theta}$ : Ground truth classifier

**SocialNet**



$$\mathbb{E}[\text{score}(\mathbf{x})|\boldsymbol{\theta}] = 6.96(\mathbf{x}^T \boldsymbol{\theta}) - 0.09$$



## 2. More Information Multinomial Logit Model

Queries must be human and mathematically interpretable

**“Select and label the most positive/negative word”**

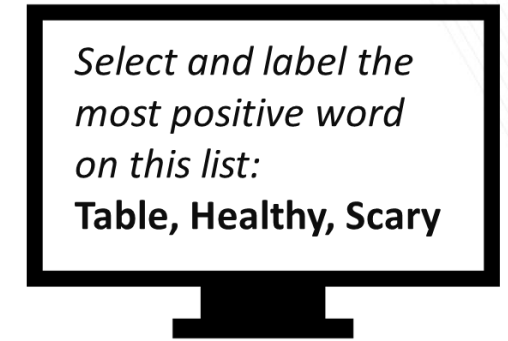
$$\left. \begin{aligned} \mathbb{P}[y = 1 | \mathbf{x}] &= \frac{1}{1 + \exp(W(\boldsymbol{\theta}^T \mathbf{x}))}, \text{ with } W \in \mathbb{R}. \\ \mathbb{P}[\mathbf{x}_i | \{\mathbf{x}_j\}_{j=1}^N, \boldsymbol{\theta}] &= \frac{\exp(u(\mathbf{x}_i, \boldsymbol{\theta}))}{\sum_{j=1}^N \exp(u(\mathbf{x}_j, \boldsymbol{\theta}))} \end{aligned} \right\} \text{Likelihood}$$

- Q1: Most positive

$$u(\mathbf{x}, \boldsymbol{\theta}) = \frac{a}{\sigma} \mathbf{x}^T \boldsymbol{\theta}$$

- Q2: Most negative

$$u(\mathbf{x}, \boldsymbol{\theta}) = -\frac{a}{\sigma} \mathbf{x}^T \boldsymbol{\theta}$$



$\mathbf{x}$ : Word embedding

$\boldsymbol{\theta}$ : Ground truth classifier

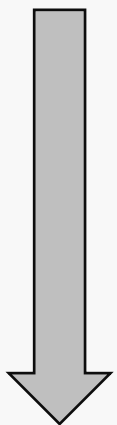
$y$ : Word label (positive: 1, negative: 0)

$u$ : Utility function (expected valence score)

## 2. More Information Multinomial Logit Model

$$\mathbb{P}[y = 1|\mathbf{x}] = \frac{1}{1+\exp(W(\boldsymbol{\theta}^T \mathbf{x}))}, \text{ with } W \in \mathbb{R}.$$
$$\mathbb{P}[\mathbf{x}_i | \{\mathbf{x}_j\}_{j=1}^N, \boldsymbol{\theta}] = \frac{\exp(u(\mathbf{x}_i, \boldsymbol{\theta}))}{\sum_{j=1}^N \exp(u(\mathbf{x}_j, \boldsymbol{\theta}))}$$

**Likelihood**



How can we get the posterior?

$$p_{\boldsymbol{\theta}} = \mathbb{P}[\boldsymbol{\theta} | \{\mathbf{x}_t, y_t, q_t, \{\mathbf{x}_j\}_{j=1}^N\}_{t=0}^i]$$

→ Approximate  $\boldsymbol{\theta}$  as a multivariate Gaussian

**Posterior over  $\boldsymbol{\theta}$**

$\mathbf{x}$ : Word embedding

$\boldsymbol{\theta}$ : Ground truth classifier

$q$ : Query

$y$ : Word label

$u$ : Utility function (expected valence score)

Slide 7 of 19

## 2. More Information Update Given Label

$$\mathbb{P}[y = 1|\mathbf{x}] = \frac{1}{1 + \exp(W(\boldsymbol{\theta}^T \mathbf{x}))}, \text{ with } W \in \mathbb{R}.$$

How do we update the posterior given the label?

Jaakkola and Jordan give a closed form approximation\*

$$\left\{ \begin{array}{l} \Sigma_{\text{pos}}^{-1} = \Sigma^{-1} + 2 \frac{\tanh(\xi/2)}{4\xi} W^2 \mathbf{x}_i \mathbf{x}_i^T \\ \boldsymbol{\mu}_{\text{pos}} = \Sigma_{\text{pos}} \left[ \Sigma^{-1} \boldsymbol{\mu} + \left( y_i - \frac{1}{2} \right) W \mathbf{x}_i \right] \\ \xi^2 = W^2 \mathbf{x}_i^T \Sigma_{\text{pos}} \mathbf{x}_i + W^2 (\mathbf{x}_i^T \boldsymbol{\mu}_{\text{pos}})^2 \end{array} \right.$$

*\*Bayesian parameter estimation via variational methods – Jaakkola and Jordan, 2000*

$\mathbf{x}$ : Word embedding

Prior:  $\mathcal{N}(\boldsymbol{\mu}, \Sigma)$

$\boldsymbol{\theta}$ : Ground truth classifier

$y$ : Word label

Posterior:  $\mathcal{N}(\boldsymbol{\mu}_{\text{pos}}, \Sigma_{\text{pos}})$



## 2. More Information Update Given Word

$$\mathbb{P} [\mathbf{x}_i | \{\mathbf{x}_j\}_{j=1}^N, \boldsymbol{\theta}] = \frac{\exp(K \mathbf{x}_i^T \boldsymbol{\theta})}{\sum_{j=1}^N \exp(K \mathbf{x}_j^T \boldsymbol{\theta})}$$

How do we update the posterior given the word selected?

$$ELBO(q) = -\text{KL}(q(\boldsymbol{\theta}) \| p(\boldsymbol{\theta})) + \mathbb{E}_{\boldsymbol{\theta} \sim q} [K \mathbf{x}_s^T \boldsymbol{\theta}] - \mathbb{E}_{\boldsymbol{\theta} \sim q} \left[ \log \sum_{j=1}^{|\mathcal{S}|} \exp(K \mathbf{x}_j^T \boldsymbol{\theta}) \right]$$

$$\rightarrow \text{KL}(q \| p) = \frac{1}{2} \left[ \log \frac{|\Sigma_p|}{|\Sigma_q|} - d + (\boldsymbol{\mu}_q)^T \Sigma_p^{-1} (\boldsymbol{\mu}_q) + (\boldsymbol{\mu}_p)^T \Sigma_p^{-1} (\boldsymbol{\mu}_p) - 2(\boldsymbol{\mu}_q)^T \Sigma_p^{-1} (\boldsymbol{\mu}_p) + \text{tr} \{ \Sigma_p^{-1} \Sigma_q \} \right]$$

$$\rightarrow \mathbb{E}_{\boldsymbol{\theta} \sim q} [K \mathbf{x}_s^T \boldsymbol{\theta}] = K \mathbf{x}_s^T \boldsymbol{\mu}_q$$

$$\rightarrow \mathbb{E}_{\boldsymbol{\theta} \sim q} \left[ \log \sum_{j=1}^{|\mathcal{S}|} \exp(K \mathbf{x}_j^T \boldsymbol{\theta}) \right] \geq \log \sum_{j=1}^{|\mathcal{S}|} \exp(K \mathbf{x}_j^T \boldsymbol{\mu}_q + 0.5 \mathbf{x}_j^T \Sigma_q \mathbf{x}_j) \quad [\text{Braun and McAuliffe, 2007}]$$

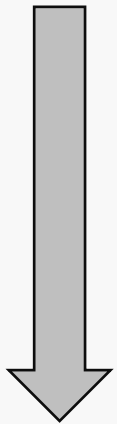
$p(\boldsymbol{\theta}) \sim \mathcal{N}(\boldsymbol{\mu}_p, \Sigma_p)$ : Prior

$q(\boldsymbol{\theta}) \sim \mathcal{N}(\boldsymbol{\mu}_q, \Sigma_q)$ : Variational Distribution

## 2. More Information Multinomial Logit Model

$$\mathbb{P} [\mathbf{x}_i | \{\mathbf{x}_j\}_{j=1}^N, \boldsymbol{\theta}] = \frac{\exp(u(\mathbf{x}_i, \boldsymbol{\theta}))}{\sum_{j=1}^N \exp(u(\mathbf{x}_j, \boldsymbol{\theta}))}$$
$$\mathbb{P} [y = 1 | \mathbf{x}] = \frac{1}{1 + \exp(W(\boldsymbol{\theta}^T \mathbf{x}))}, \text{ with } W \in \mathbb{R}.$$

} **Likelihood**



**Variational inference**

**Posterior over  $\theta$**

$\mathbf{x}$ : Word embedding

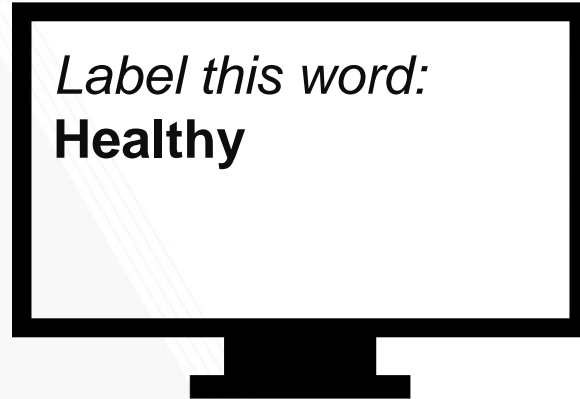
$\boldsymbol{\theta}$ : Ground truth classifier

$y$ : Word label (positive: 1, negative: 0)

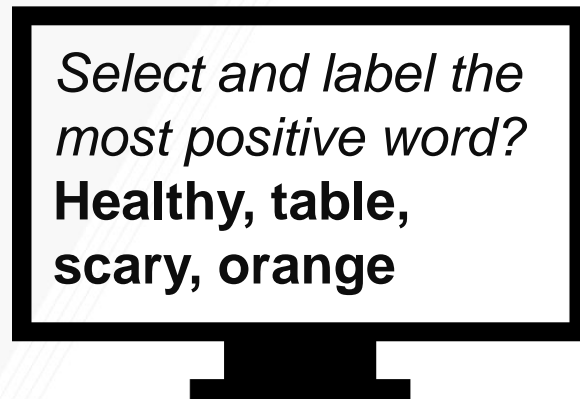
$u$ : Utility function (expected valence score)

## 2. More Information Experiments

Label:



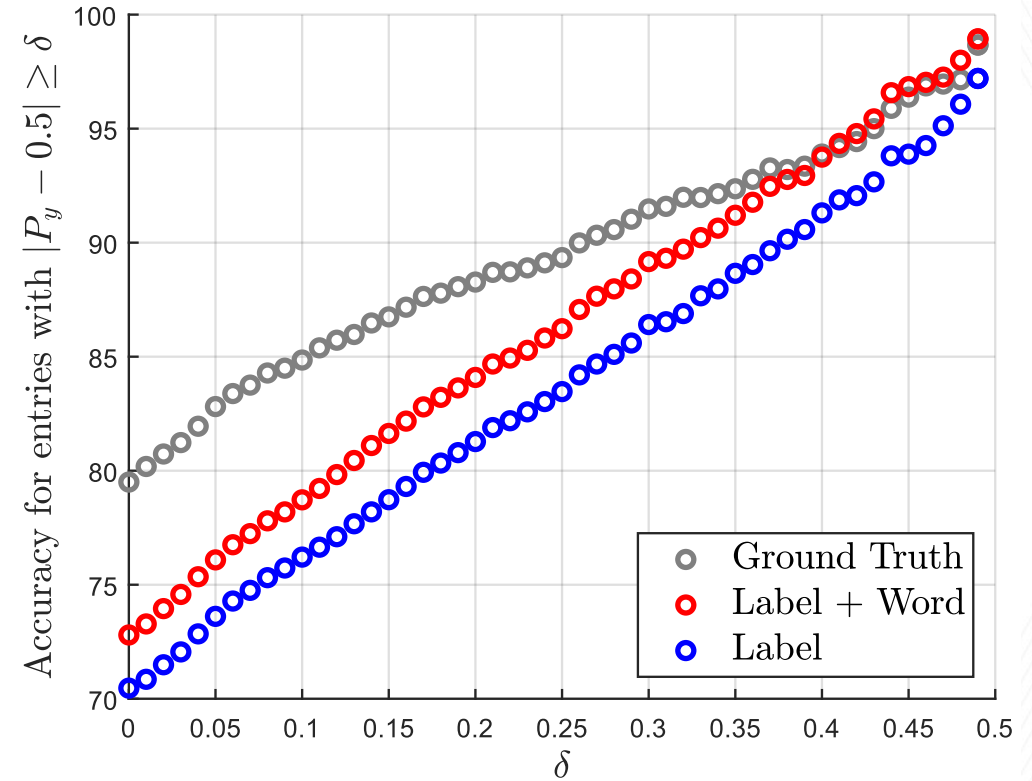
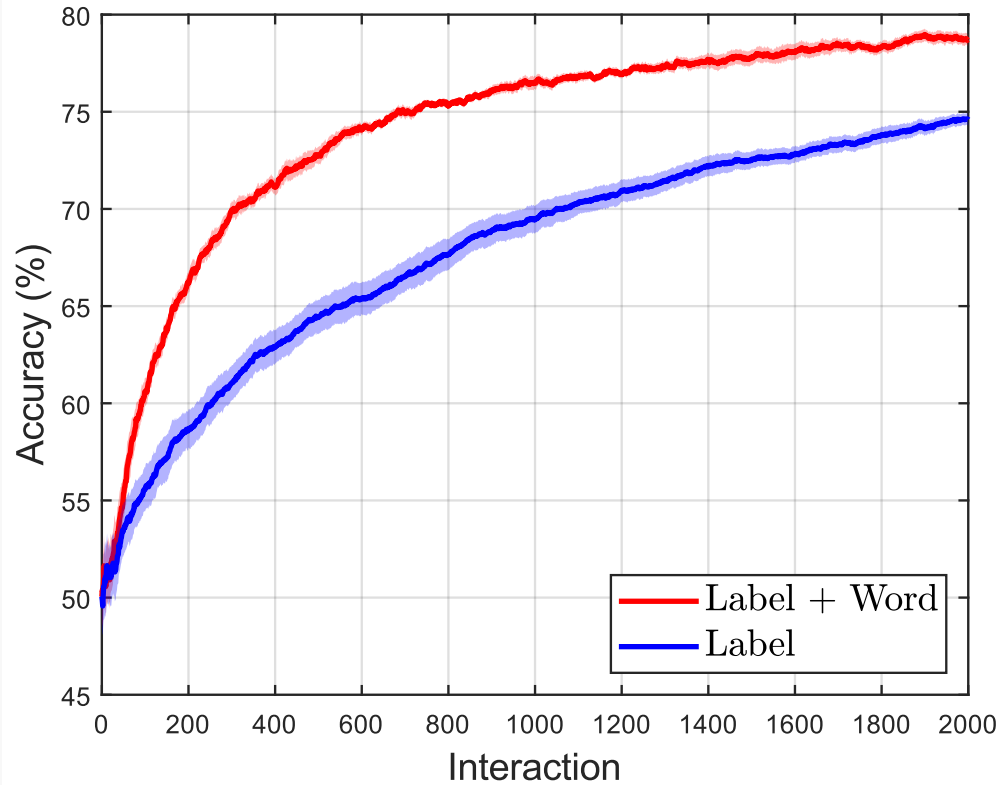
Label + Word:



### NRC-VAD Lexicon dataset:

Each word  $\mathbf{x}$  has a valence score mean  $\mu_{\mathbf{x}}$  and variance  $\sigma_{\mathbf{x}}^2 \rightarrow \text{score: } s_{\mathbf{x}} \sim \mathcal{N}(\mu_{\mathbf{x}}, \sigma_{\mathbf{x}}^2)$

## 2. More Information Empirical Results



## 2. More Information Theoretical Results

### Under Assumptions

1. Word and label selected are independent of the history given the classifier

$$p(\mathbf{x}_t, y_t | \boldsymbol{\theta}, q_t, \mathcal{S}_t, \mathcal{F}_{t-1}) = p(\mathbf{x}_t, y_t | \boldsymbol{\theta}, q_t, \mathcal{S}_t)$$

2. The label only depends on the word it is referring to

$$p(y_t | \mathbf{x}_t, q_t, \mathcal{S}_t) = p(y_t | \mathbf{x}_t)$$

3. An answer always provides some information

$$I(\boldsymbol{\theta}; X_t, Y_t | \mathcal{F}_{t-1}) \geq L > 0$$

### Simplified Theorem

The expected stopping time  $T_\epsilon = \min\{t : |\boldsymbol{\Sigma}_{\boldsymbol{\theta} | \mathcal{F}_t}|^{1/d} < \epsilon\}$  is bounded as

$$\frac{d}{2} \frac{\log_2 \frac{2}{\pi \epsilon \epsilon}}{\log_2 2^{|\mathcal{S}|}} \leq \mathbb{E}[T_\epsilon] \leq \frac{d}{2L} \log_2 \frac{e^4 d^2}{2\sqrt{2}(d+2)\epsilon} - 1.$$

where  $\mathbf{x} \in \mathbb{R}^d$  and  $\mathcal{S} = \{\mathbf{x}_j\}_{j=1}^{|\mathcal{S}|}$  are the candidate words.

## 2. More Information Theoretical Results

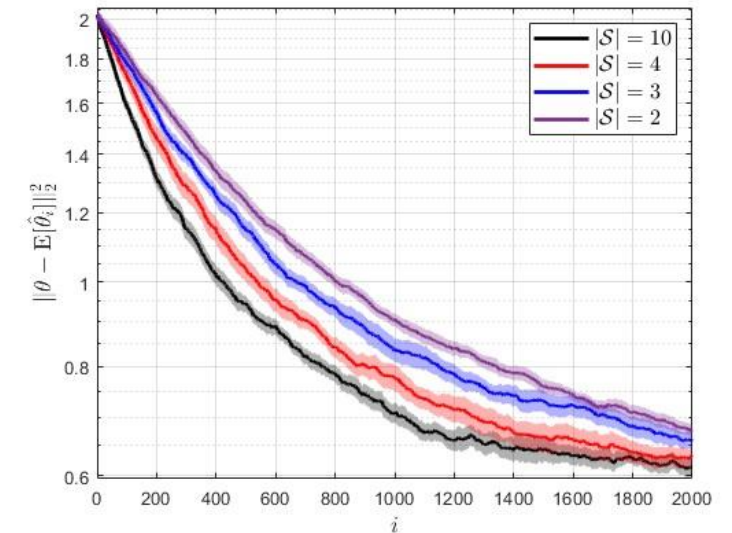
### Simplified Theorem

The expected stopping time  $T_\epsilon = \min\{t : |\Sigma_{\theta|_{\mathcal{F}_t}}|^{1/d} < \epsilon\}$  is bounded as

$$\frac{d}{2} \frac{\log_2 \frac{2}{\pi e \epsilon}}{\log_2 2|\mathcal{S}|} \leq \mathbb{E}[T_\epsilon] \leq \frac{d}{2L} \log_2 \frac{e^4 d^2}{2\sqrt{2}(d+2)\epsilon} - 1.$$

where  $\mathbf{x} \in \mathbb{R}^d$  and  $\mathcal{S} = \{\mathbf{x}_j\}_{j=1}^{|\mathcal{S}|}$  are the candidate words.

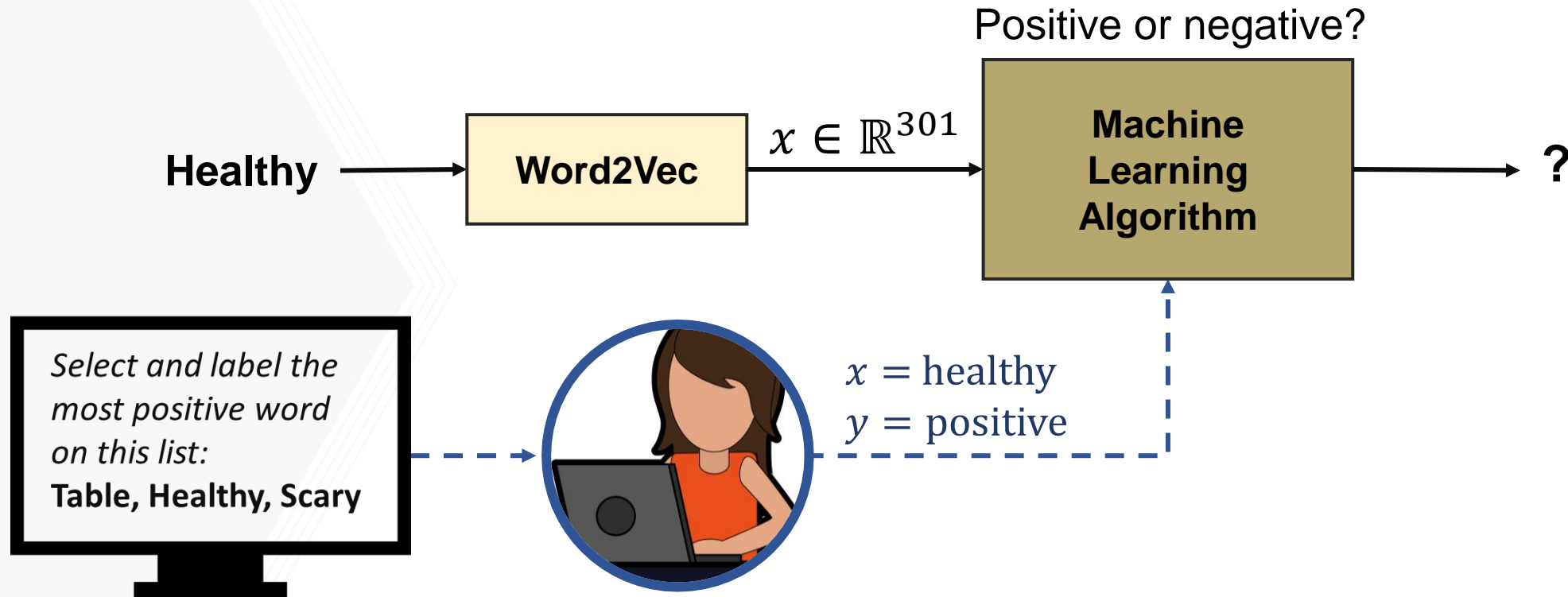
- ✓ The number of question to ask the human to reach uncertainty  $< \epsilon$  is on the order of  $\log 1/\epsilon$
- ✓ Related to the error  $\text{MSE}_t = \text{trace}(\Sigma_{\theta|_{\mathcal{F}_t}}) \geq d|\Sigma_{\theta|_{\mathcal{F}_t}}|^{1/d}$
- ✓ The more words in the list, the faster the error decays





## 2. More Information Motivation

How can ML algorithms learn to classify words **without exhausting human patience?**



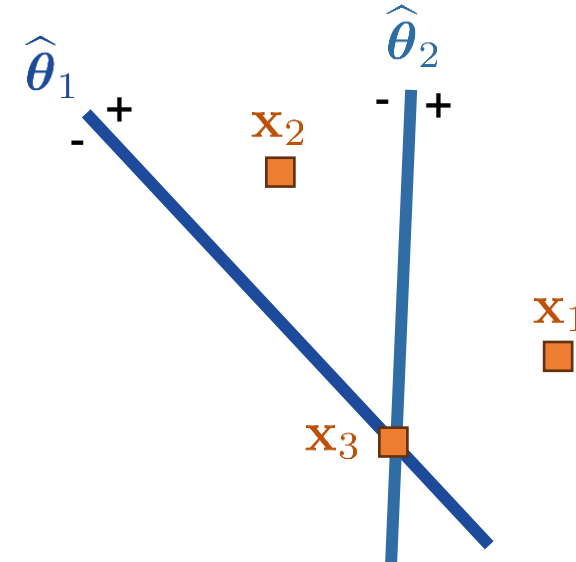
- ✓ Could we get **more information** from the human?
- ❑ Could we get the information **faster**?

### 3. Faster Active Learning Heuristic



Instead of showing the humans a random list of words, could we select them in a smart way?

Example	$P[+ x, \theta = 1]$	$P[+ x, \theta = 2]$
$x_1$	0.99	0.99
$x_2$	0.99	0.01
$x_3$	0.5	0.5



Heuristic in AL:

$$\operatorname{argmax}_{\mathbf{x}} \underbrace{H(\mathbb{E}_{\theta}[f_{\theta}(\mathbf{x})])}_{\text{Maximize uncertainty of the expected output}} - \underbrace{\mathbb{E}_{\theta}[H(f_{\theta}(\mathbf{x}))]}_{\text{Minimize uncertainty due to noise}}$$

→ Maximize uncertainty of the expected output

→ Minimize uncertainty due to noise

$H$ : Entropy     $\theta$ : Ground truth classifier     $\mathbf{x}$ : Word embedding

### 3. Faster Active Word Selection

Heuristic:

$$\mathcal{S} = \operatorname{argmax}_{\mathcal{S} \in \{\mathcal{X}\}^k} \underbrace{H(\mathbb{E}_{\boldsymbol{\theta}}[\mathbf{x}_i, y_i \mid q, \boldsymbol{\theta}, \mathcal{S}])}_{\text{Maximize uncertainty of the expected output}} - \underbrace{\mathbb{E}_{\boldsymbol{\theta}}[H(\mathbf{x}_i, y_i \mid q, \boldsymbol{\theta}, \mathcal{S})]}_{\text{Minimize uncertainty due to noise}}$$

→ Maximize uncertainty of the expected output

→ Minimize uncertainty due to noise

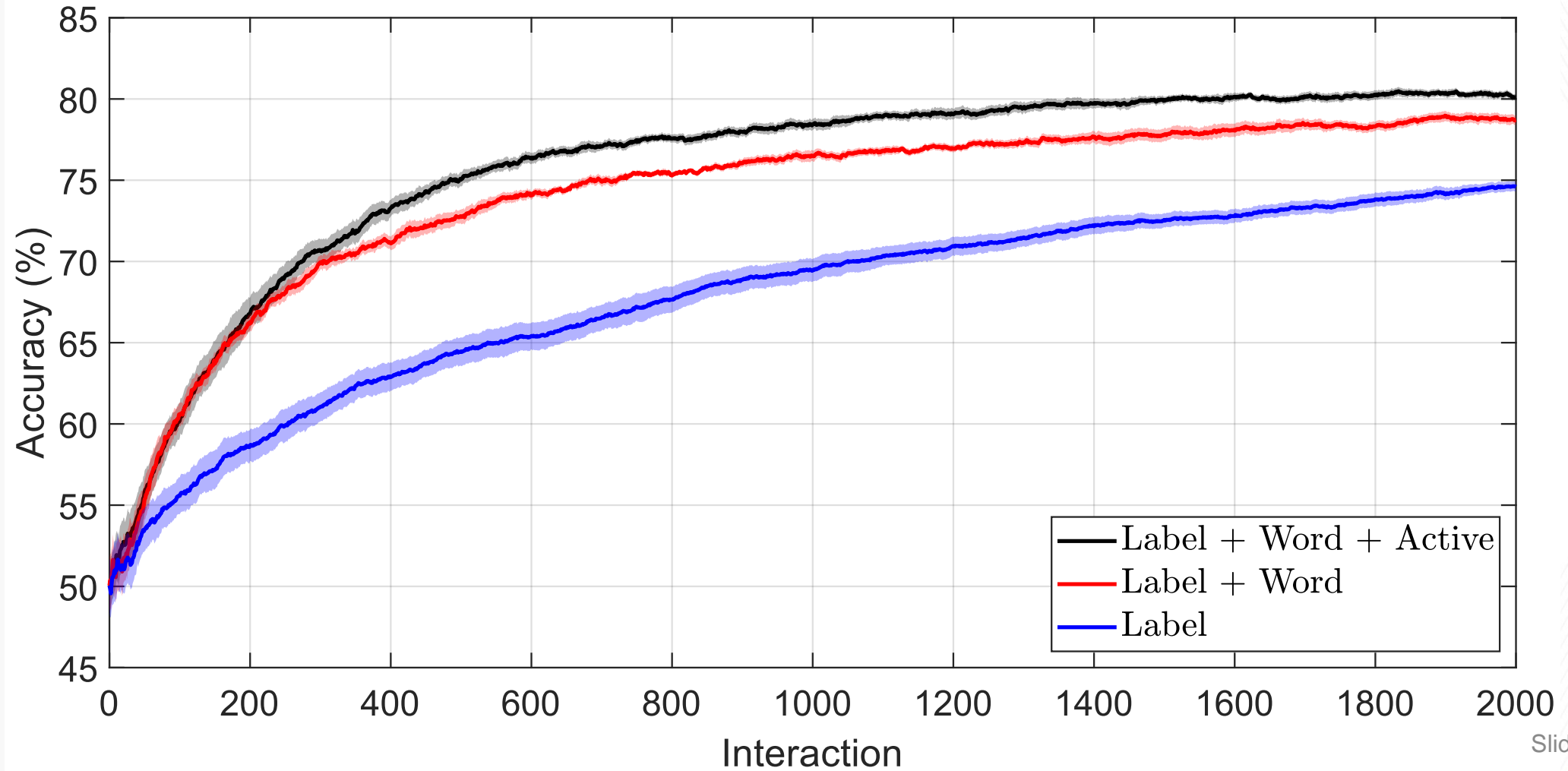
Problem: There exist combinatorically many sets  $\binom{|\mathcal{X}|}{|\mathcal{S}|}$  to maximize over

Our Approach: Greedily select one word at a time

If  $|\mathcal{X}| = 3500$  and  $|\mathcal{S}| = 4$ :  
 $\binom{|\mathcal{X}|}{|\mathcal{S}|} \sim 10^{15}$   
Galaxies  $\sim 10^{12}$   
If each computation 1ms,  
 $t \sim 31,7000$  years

$H$ : Entropy    $\boldsymbol{\theta}$ : Ground truth classifier    $\mathbf{x}$ : Word embedding    $y$ : Word label

### 3. Faster Results



## 4. Summary

1. We introduce a novel **human response model**.
2. We **speed up learning** in sentiment classification
  - By combining label requests with word selection.
  - By active query selection.
3. We **validate** our approach
  - Theoretically: Bounds for expected stopping time.
  - Empirically: Experiments with human data.



# Enhancing Human-in-the-Loop Learning for Binary Sentiment Word Classification

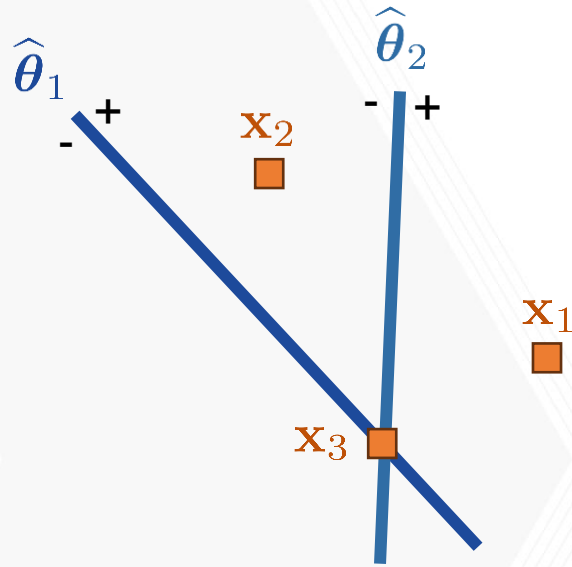
Belén Martín-Urcelay, Christopher R. Rozell, Matthieu R. Bloch

December 17, 2024





### 3. Faster Active Learning Heuristic



Example	$P[+ x, \theta = 1]$	$P[+ x, \theta = 2]$
$x_1$	0.99	0.99
$x_2$	0.99	0.01
$x_3$	0.5	0.5

$$x_1 \rightarrow H(0.99) - [0.5 (H(0.99) + H(0.99))] = 0.02 - 0.02 = 0$$

$$x_2 \rightarrow H(0.5) - [0.5 (H(0.01) + H(0.99))] = 1 - 0.02 = 0.98$$

$$x_3 \rightarrow H(0.5) - [0.5 (H(0.5) + H(0.5))] = 1 - 1 = 0$$

Heuristic in AL:

$$\operatorname{argmax}_{\mathbf{x}} \underbrace{H(\mathbb{E}_{\theta} [f_{\theta}(\mathbf{x})])}_{\text{Maximize uncertainty of the expected output}} - \underbrace{\mathbb{E}_{\theta} [H(f_{\theta}(\mathbf{x}))]}_{\text{Minimize uncertainty due to noise}}$$

→ Maximize uncertainty of the expected output

→ Minimize uncertainty due to noise

$H$ : Entropy     $\theta$ : Ground truth classifier     $\mathbf{x}$ : Word embedding